

# Evidence for leptonic CP phase from $\text{NO}\nu\text{A}$ , T2K and ICAL

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## Abstract

The phenomenon of neutrino oscillation is now well understood from the solar, atmospheric, reactor and accelerator neutrino experiments. This oscillation is characterized by a unitary PMNS matrix which is parametrized by three mixing angles and one phase known as the leptonic CP phase. Though there are already significant amount of information about the three mixing angles but the CP phase is still unknown. The long baseline experiments(LBL) have CP sensitivity coming from the appearance channel but atmospheric neutrinos known to have negligible CP sensitivity. In this work we study the synergy between the LBL experiment  $\text{NO}\nu\text{A}$ , T2K and the atmospheric neutrino experiment ICAL@INO for obtaining the first hint of CP violation in the lepton sector. We find that due to the lack of knowledge of hierarchy and octant CP sensitivity of  $\text{NO}\nu\text{A}$ /T2K is poorer for some parameter ranges. Addition of ICAL data to T2K and  $\text{NO}\nu\text{A}$  can exclude these spurious wrong-hierarchy and/or wrong-octant solutions and cause a significant increase in the range of  $\delta_{CP}$  values for which a hint of CP violation can be achieved. Similarly the precision with which  $\delta_{CP}$  can be measured also improves with inclusion of ICAL data.

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## I. INTRODUCTION

CP symmetry refers to invariance under simultaneous transformation of charge conjugation and parity. CP violation has been observed in the quark sector and this can be explained by the complex phase of the CKM matrix [1]. The complex phase, analogous to the CKM phase, in the leptonic mixing matrix can lead to CP violation in the lepton sector [2]. However experimental detection of this phase is necessary to establish this expectation on a firm footing. The determination of the leptonic CP phase is interesting not only in the context of fully determining the PMNS mixing matrix but also because it could be responsible for the observed matter-antimatter asymmetry through the mechanism of leptogenesis [3].

A potential problem in determining  $\delta_{CP}$  comes from the lack of knowledge of hierarchy and octant which gives rise to fake solutions coming from wrong hierarchy and wrong octant. A prior knowledge of hierarchy and octant can help to eliminate these fake solutions thereby enhancing the CP sensitivity. Since the baselines of the current superbeam experiments T2K and NO $\nu$ A are not too large they have limited hierarchy and octant sensitivity and thus causing a significant fall in the CP sensitivity. On the other hand, the hierarchy and octant sensitivity of atmospheric neutrino experiments is independent of  $\delta_{CP}$  [4]. Hence, a combination of long-baseline (LBL) and atmospheric data can substantially improve the ability of the LBL experiments to measure  $\delta_{CP}$ . In this work we demonstrate that the CP sensitivity of T2K and NO $\nu$ A can be enhanced significantly by including atmospheric neutrino data in the analysis. For the latter we consider a magnetized iron calorimeter detector (ICAL) which is being developed by the INO collaboration [5].

## II. THE APPEARANCE CHANNEL

In matter of constant density,  $P_{\mu e}$  can be expressed in terms of the small parameters  $\alpha = \Delta_{21}/\Delta_{31}$  and  $s_{13}$  as [6]

$$P_{\mu e} = 4s_{13}^2 s_{23}^2 \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} + \alpha \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos(\Delta - \delta_{CP}) \times \frac{\sin \hat{A}\Delta \sin[(1 - \hat{A})\Delta]}{\hat{A} (1 - \hat{A})} + \mathcal{O}(\alpha^2), \quad (1)$$

where  $\Delta = \Delta_{31}L/4E$ ,  $s_{ij}(c_{ij}) \equiv \sin\theta_{ij}(\cos\theta_{ij})$ ,  $\hat{A} = 2\sqrt{2}G_F n_e E/\Delta_{31}$ ,  $G_F$  is the Fermi constant and  $n_e$  is the electron number density. For neutrinos, the signs of  $\hat{A}$  and  $\Delta$  are positive for NH and negative for IH and vice-versa for antineutrinos. We can see that CP appears in the subleading second term in Eq. 1 which is also the source of the hierarchy- $\delta_{CP}$  degeneracy [7].

## III. EXPERIMENTAL SPECIFICATION

For the long-baseline experiments NO $\nu$ A and T2K, simulation is done using the GLOBES package [8]. T2K (L = 295 Km) is assumed to have a 22.5 kt Water Čerenkov detector running effectively for  $5(\nu) + 0(\bar{\nu})$  years. For NO $\nu$ A (L = 812 Km), we consider a 14 kt

TASD detector running for  $5(\nu) + 5(\bar{\nu})$  years. Detailed specifications of these experiments are given in [9, 10].

For atmospheric neutrinos we consider ICAL@INO, which is capable of detecting muon events with charge identification, with a proposed mass of 50 kT [5]. For our analysis we use neutrino energy and angular resolutions of  $(10\%, 10^\circ)$ .

#### IV. CPV DISCOVERY POTENTIAL OF $\text{NO}\nu\text{A}$ , T2K AND ICAL

The discovery potential of an experiment for CP violation is defined by

$$\chi^2 = \min \frac{(N_{ex}(\delta_{CP}^{tr}) - N_{th}(\delta_{CP}^{test} = 0, 180^\circ))^2}{N_{ex}(\delta_{CP}^{tr})} \quad (2)$$

where  $N_{ex}$  and  $N_{th}$  are the true and test events respectively.

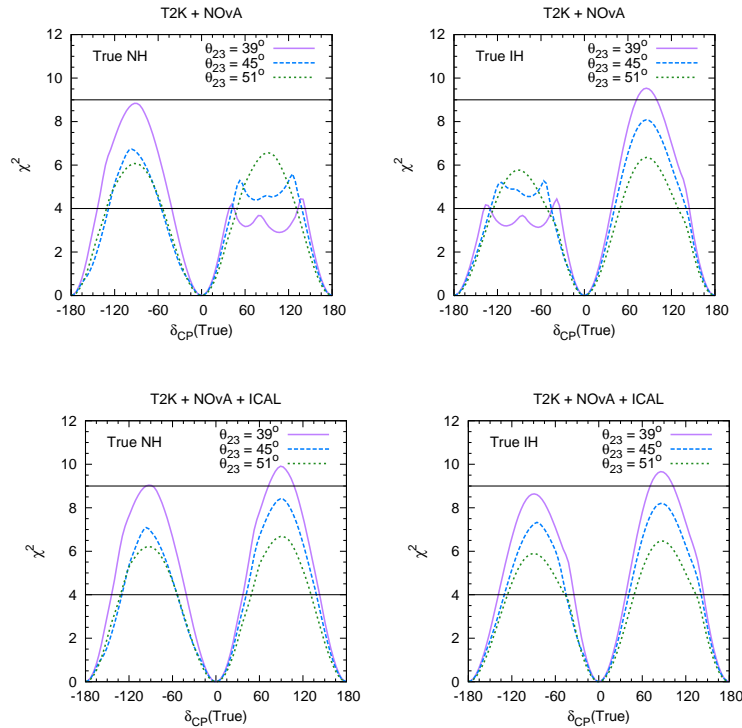


FIG. 1: CPV discovery vs true  $\delta_{CP}$  for  $\text{NO}\nu\text{A}+\text{T2K}$  (upper row) and  $\text{NO}\nu\text{A}+\text{T2K}+\text{ICAL}$  (lower row), for three values of  $\theta_{23}$ ,  $\sin^2 2\theta_{13} = 0.1$  and a true normal (left panels) or inverted (right panels) mass hierarchy, with 500 kT yr exposure for ICAL

From the upper panels of Fig 1 it may be observed that the CPV discovery of  $\text{NO}\nu\text{A}+\text{T2K}$  suffers a drop in the region  $+90^\circ$  if it is NH, and  $-90^\circ$  if it is IH. This is due to the fact that the minimum for CPV discovery occur in the wrong hierarchy. In atmospheric neutrinos the baselines are related to the zenith angle  $\theta_z$ . As the  $\delta_{CP}$  term always appears along with a factor of  $\cos \Delta$  or  $\sin \Delta$ , even a 10% error range in  $\theta_z$  this oscillating term varies over an

entire cycle. As a result, the  $\delta_{CP}$ -sensitivity gets washed out. Thus atmospheric neutrino experiments by themselves are not sensitive to  $\delta_{CP}$  but gives a hierarchy sensitivity due to large matter effect. This hierarchy sensitivity can exclude the wrong-hierarchy solutions and this is shown in lower panels of Fig 1 that when ICAL is added to NO $\nu$ A+T2K, the drop in the CPV discovery is resolved. The results depend significantly on the true value of  $\theta_{23}$ . As  $\theta_{23}$  increases, hierarchy sensitivity increases but CP sensitivity decreases. As a result for  $\theta_{23} = 51^\circ$ , the  $\chi^2$  minima for NO $\nu$ A+T2K comes in the correct hierarchy and the ICAL information becomes superfluous.

## V. CP PRECISION OF NO $\nu$ A, T2K AND ICAL

The the precision  $\chi^2$  is defined as

$$\chi^2 = \min \frac{(N_{ex}(\delta_{CP}^{tr}) - N_{th}(\delta_{CP}^{test}))^2}{N_{ex}(\delta_{CP}^{tr})} \quad (3)$$

In Fig. 2, we plot the CP precision in  $\delta_{CP}(\text{true})$  vs  $\delta_{CP}(\text{test})$  plane for NO $\nu$ A, T2K and ICAL. In this figures we have used  $\sin^2 \theta_{23} = \sin^2 \theta_{\mu\mu} / \cos^2 \theta_{13}$  to take care of the intrinsic octant degeneracy that arises at  $\theta_{\mu\mu}$  and  $90^\circ - \theta_{\mu\mu}$  in the disappearance channel. The allowed values

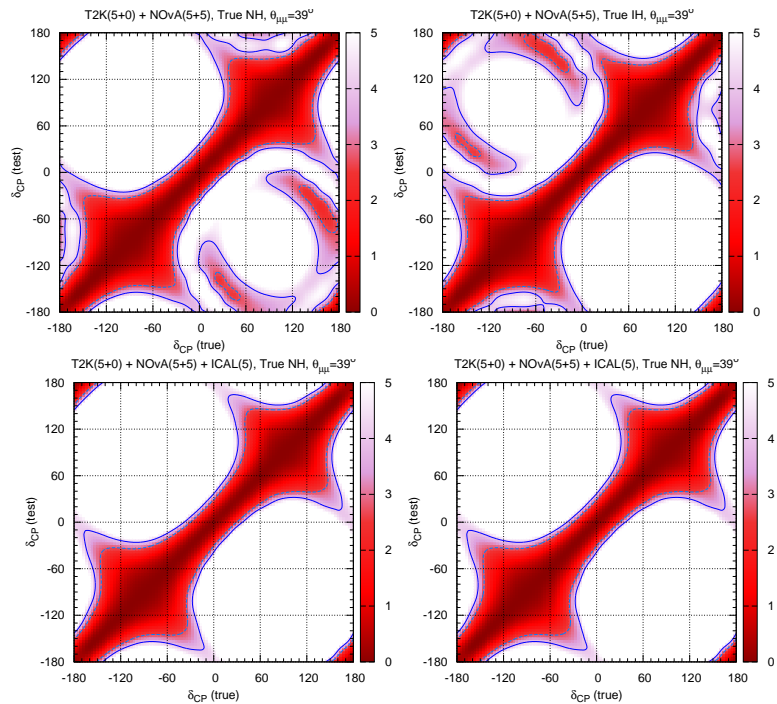


FIG. 2: CP precision at 90%/95% C.L. for NO $\nu$ A+T2K (upper row) and NO $\nu$ A+T2K+ICAL (lower row), for  $\theta_{23} = 39^\circ$ ,  $\sin^2 2\theta_{13} = 0.1$  and a true normal (left panels) or inverted (right panels) mass hierarchy, with 250 kT yr exposure for ICAL

of  $\delta_{CP}$  are represented by the shaded regions. For an ideal measurement, the allowed values would be very close to the true value. However, due to the hierarchy- $\delta_{CP}$  degeneracy, we see that for NO $\nu$ A+T2K, other  $\delta_{CP}$  values are also getting allowed (upper panels of Fig 2).

However addition of 5 years of ICAL data is sufficient enough to rule out those degenerate allowed regions to give a finer CP precision(lower panels of Fig 2) though it should be noted that the act of adding ICAL data does not help in the diagonal regions.

## VI. $\theta_{13}$ AND $\theta_{23}$ DEPENDENCE IN CPV DISCOVERY $\chi^2$

As seen in Eqn.1,  $P_{\mu e}$  has a leading order CP dependent term  $\sim \sin^2 \theta_{13} \sin^2 \theta_{23}$  and a sub-leading CP independent term  $\sim \sin 2\theta_{13} \sin 2\theta_{23}$ . Thus  $\theta_{13}$  and  $\theta_{23}$  is expected to have similar dependence on  $\delta_{CP}$ . For illustrative purposes, the CP  $\chi^2$  can be written as

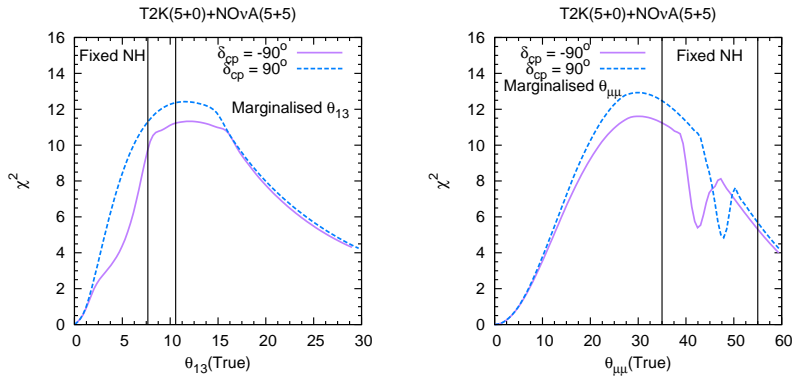


FIG. 3: CP violation discovery potential of NO $\nu$ A+T2K as a function of true  $\theta_{i3}$  and a fixed NH is assumed

$$\chi^2 \sim \frac{P(\delta_{CP}) \sin^2 2\theta_{i3}}{Q \sin^2 \theta_{i3} + R(\delta_{CP}) \sin 2\theta_{i3}}, \quad (4)$$

where  $P$ ,  $Q$ ,  $R$  are functions of the other oscillation parameters apart from  $\delta_{CP}$  and  $i=1,2$ . For small values of  $\theta_{i3}$ ,  $\chi^2 \sim \theta_{i3}$  which is an increasing function and when  $\theta_{i3}$  is close to  $90^\circ$   $\chi^2 \sim (90^\circ - \theta_{i3})^2$  which decreases with  $\theta_{i3}$ . Therefore, CP sensitivity initially increases with  $\theta_{i3}$ , peaks at an optimal value, and then decreases with  $\theta_{i3}$ .

These features are clearly reflected in Fig. 3. The left panel shows that the sensitivity to CP violation is maximum for NO $\nu$ A+T2K in the current  $3\sigma$  range of  $\theta_{13}$ (region between the vertical black lines). From the right panel we find that for  $40^\circ < \theta_{\mu\mu}^{tr} < 49^\circ$ , there is a wiggle signaling the octant- $\delta_{CP}$  degeneracy. The behaviour is different for  $\delta_{CP}^{tr} = \pm 90^\circ$  depending on the true octant. This is illustrated in Fig. 4. where we can notice a drop at  $-90^\circ$  for  $\theta_{\mu\mu} = 43^\circ$  and at  $+90^\circ$  for  $\theta_{\mu\mu} = 49^\circ$  for NO $\nu$ A+T2K when the octant is assumed to be unknown. But when ICAL is added, it restricts the  $\delta_{CP}$ -octant degeneracy to  $41 < \theta_{\mu\mu} < 48$ . Thus we can see a partial improvement at  $\theta_{\mu\mu} = 43^\circ$  but the degeneracy is fully resolved at  $\theta_{\mu\mu} = 49^\circ$  with the help of ICAL.

## VII. CONCLUSION

In this work we have studied CP sensitivity of the current and upcoming long-baseline experiments T2K and NO $\nu$ A and the atmospheric neutrino experiment ICAL@INO. We

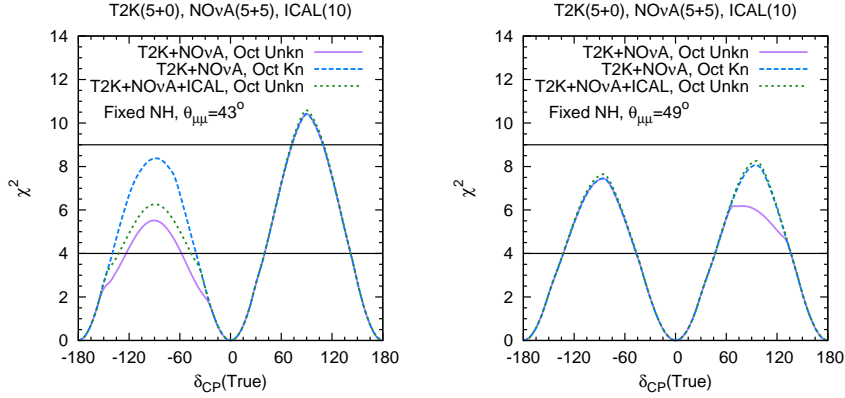


FIG. 4: CP violation discovery potential of NO $\nu$ A, T2K and ICAL as a function of true  $\delta_{CP}$  for  $\theta_{\mu\mu}^{tr} = 43^\circ$  (left panel) and  $49^\circ$  (right panel).  $\sin^2 2\theta_{13}^{tr} = 0.1$  and a fixed NH is assumed

see that due to hierarchy- $\delta_{CP}$  degeneracy, there is a drop in CP sensitivity for NO $\nu$ A and T2K in the degenerate region. The main role of the atmospheric data is to exclude the wrong hierarchy solutions to lift the degeneracy in the unfavourable parameter regions for T2K/NO $\nu$ A. We have also shown that the current values of  $\theta_{13}$  lies in a region where CP sensitivity is maximum. There is also a degeneracy of  $\delta_{CP}$  with the octant in the range  $40^\circ < \theta_{\mu\mu}^{tr} < 49^\circ$  for T2K+NO $\nu$ A. Addition of ICAL data helps to restrict the degeneracy at  $41^\circ < \theta_{\mu\mu}^{tr} < 48^\circ$ .

More detailed discussions and results can be found in [11, 12] on which this article is based.

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